A Time-dependent Multi-reference Unified Cluster Cumulant Formulation to Study the Subdynamics of Quantum System Coupled both to Thermal and Stochastic Bath

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Abstract

This is to introduce a time-local effective hamiltonian unified cluster cumulant method based on the Time-dependent Multi-reference Cluster Cumulant (TDMRCC) and Thermal Cluster Cumulant (TCC) strategy developed by Mukherjee and his coworkers [13-17]. A factorized ansatz for $U_I P = [U_I]_{ex} [U_I]_M P$ with $P = |\varphi_i \rangle \otimes |0_\beta \rangle \otimes |0_f \rangle$, where $|\varphi_i \rangle$, $|0_\beta \rangle$ and $|0_f\rangle$ denote the purely quantum mechanical vacuum state, the thermal vacuum state, the base state for the solvent degrees of freedom respectively, and $[U_I]_{ex}$ consists of operators admixing the thermally as well as the stochastically projected model space functions with that of the virtual space outside the model space whose functions govern the time-evolution of $[U_I]_M$ via the time-local effective operator, $V_{eff}[\beta,\xi,t] (= \langle V_I[U_I]_{ex} >_{\beta} \rangle_f)$, where $\langle \cdots \rangle_{\beta}$ and $< \cdots >_{f}$ denote thermal and stochastic averaging respectively. The exponential ansatz is introduced both for $[U_I]_{ex}$ and $[U_I]_M$ and these ansatze are normal ordered with respect to both the thermal and the stochastic variables, i.e., $[U_I]_{ex} = \left\{ \left\{ e^{S_{m,n}^f} \right\}_{\beta} \right\}_f$ and $[U_I]_M = \{ e^{X_{k,k}} \}_{\beta}$. The averaged evolution operator, $\langle U_I(t) \rangle_{\beta} \rangle_f$ with respect to both the thermal boson variables in thermal equilibrium and the stochastic variables is obtained. Finally, the mathematical expression for the second order cluster cumulant $[X_{0,0}]^{(2)}$ is derived for a quantum particle trapped in a 1-dimensional anharmonic oscillator potential coupled both to the stochastic and thermal baths.